

$$A_{\Sigma}^T = \frac{m^2 g^2 t_k^2}{2m} = \frac{mgh}{\sin^2 \alpha (1 - \mu / \operatorname{tg} \alpha)} \quad (6)$$

At factor of friction  $\mu = 0$  we receive a parity (3). The relation of work with friction  $A_{\Sigma}^T$  to work of gravity  $A_{\Sigma}$  in the absence of a friction depending on relation  $\mu / \operatorname{tg} \alpha$  are resulted in table 1.

$\mu / \operatorname{tg} \alpha$	0	0,2	0,4	0,5	0,6	0,7	0,8	0,9	0,95
$A_{\Sigma}^T / A_{\Sigma}$	1	1,25	1,667	2	2,5	3,33	5	10	20

At factor of friction  $\mu = 0,9 \operatorname{tg} \alpha$  and coal  $\alpha = 10^\circ$  work of gravity  $A_{\Sigma}^T \cong 330mgh$ .

More detailed conclusion of formulas for calculation of work of various forces is resulted in [1,2].

#### References

1. Ivanov E.M. Work and energy in the classical mechanics and the first law of thermodynamics. Dimitrovgrad: DITUD UIGTU, 2004.
2. Ivanov E.M. Work of centripetal and gyroscopic Forces.//European Journal Natural History, 2006, #1, p.80.

### WORK OF TURN AND WORK OF CENTRIPETAL FORCES

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Turn work is a work, which needs to be spent to change a direction of movement of a body (to turn a vector of speed  $V_0$  on some corner  $\alpha$ ):

$$A_{\alpha} = \frac{I_2^2}{2m} = \frac{I_0^2}{m} (1 - \cos \alpha)$$

where  $I_0 = mV_0$  - a body impulse. Under the same formula work of centripetal force pays off.

From the law of inertia Galilee (Newton's I law) follows, that any body shows resistance at attempts to set it in motion or to change the module or the DIRECTION of its speed. This property of bodies is called as inertness. To overcome resistance, it is necessary to make effort, i.e. to make work. The formula for calculation of work of change of speed of a body is resulted in all textbooks of physics. It is received on the basis of Newton's

II law for a resultant of force  $F_a = \sum F_i = ma$  in a kind

$$A = F_a \cdot S \quad (1)$$

As way  $S = at^2 / 2 = Ft^2 / 2m$  it is possible to express work through an impulse of force  $I_a = F_a t$

$$A = F_a^2 t^2 / 2m = I_a^2 / 2m \quad (2)$$

Let's define work, which needs to be spent to change the DIRECTION of movement of a body, i.e. to turn a vector of speed  $V_0$  on some corner  $\alpha$ . The author [1-3] named its WORK of TURN. At change of

a direction of movement at  $V_0 = \text{const}$  kinetic energy of a body does not change, but work should be spent, as the body shows resistance to attempt to change a direction of its speed. Change of a direction of movement we will make at the expense of action of

INSTANT FORCE  $F_2$  for what we will direct an interval of action of force  $t \rightarrow 0$ , and size of force  $F_2 \rightarrow \infty$ . Then we will receive instant force in the

form of  $I_2 \delta(t)$ , where  $\delta(t)$  - delta-function Diraka [4].

Turn work

$$A_\alpha = \frac{I_2^2}{2m} = \frac{I_0^2}{m} (1 - \cos \alpha), 0 \leq \alpha \leq \pi \quad (3)$$

For corners of turn, big than  $\pi$ , for example  $\beta = \pi + \alpha$ , considering periodicity of function  $\cos \alpha$ , it is necessary to turn work on a corner  $180^\circ$  ( $A_\pi$ ) to add work  $A_\alpha$ . Kinetic energy of body

$K_0 = mV_0^2 / 2 = I_0^2 / 2m$ . In table 1 work of turn  $A_\alpha$  depending on corner  $\alpha$  is resulted.

$\alpha$	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$	$180^\circ$	$270^\circ$	$360^\circ$
$A_\alpha$	0	$K_0(2 - \sqrt{3})$	$K_0(2 - \sqrt{2})$	$K_0$	$2K_0$	$4K_0$	$6K_0$	$8K_0$

Thus, at turn of a body, moving on a circle, i.e. on one turn, work equal  $8K_0$  (eight kinetic энергий bodies) is spent.

In textbooks of physics for force  $F$  directed under some corner  $\alpha$  to moving  $S$ , the formula for moving work write down in a kind:  $A = F \cdot S \cos \alpha$ . In this connection assert, that the centripetal forces causing movement of a body on a circle (for example, Lorentz's force at rotary movement of a charge in a magnetic field, or force of gravitation at movement of the companion round the Earth on a circular orbit) do not make work, since they are always perpendicular to a vector of speed, and  $\cos 90^\circ = 0$ .

Companion movement is an infinite falling of a body by gravity. Companion movement to similarly movement of the body thrown from a tower in height  $h$  in a horizontal direction with initial speed  $V_0$ . At body falling to the Earth the gravity makes work  $A = mgh$ . Not clearly, why the gravity does not make work at companion movement. These processes are similar.

In work [3] conclusion of the formula for calculation of work of centripetal force  $F$  by three methods. The formula (3) as a result turns out. As  $mV_0^2 = FR$  (3) it is possible to copy in the form of  $A_\alpha = FR(1 - \cos \alpha)$ . At  $\alpha = 90^\circ$  it is received  $A_{90^\circ} = FR = FS$  - the usual formula for work, where  $S$  - the vertical moving equal to radius of an orbit. At one turn  $S = 4R$  and work will be equal  $A_{2\pi} = 4FR = 4mV_0^2 = 8K_0$ .

#### References

1. Ivanov E.M. work of centripetal and gyroscopic forces. // Bulletin DITUD, № 1.; Dimitrovgrad, 2003.
2. Ivanov E.M. Work of centripetal and gyroscopic Forces. // European Journal History, 2006, №1, p.80.
3. Ivanov E.M. work and energy in the classical mechanics and I law of thermodynamics. Dimitrovgrad: DITUD UIGTU, 2007.
4. Arfken G. Mathematical methods for physics. Academic Press. New York and London.